RINGMesh: A programming library for developing mesh-based geomodeling applications

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Abstract

RINGMesh is a C++ open-source programming library for manipulating discretized geological models. It is designed to ease the development of applications and workflows that use discretized 3D models. It is neither a geomodeler, nor a meshing software. RINGMesh implements functionalities to read discretized surface-based or volumetric structural models and to check their validity. The models can be then exported in various file formats. RINGMesh provides data structures to represent geological structural models, either defined by their discretized boundary surfaces, and/or by discretized volumes. A programming interface allows to develop new geomodeling methods, and to plug in external software. The goal of RINGMesh is to help researchers to focus on the implementation of their specific method rather than on tedious tasks common to many applications. The documented code is open-source and distributed under the modified BSD license. It is available at https://www.ring-team.org/index.php/software/ringmesh.

Keywords: Structural model, Geology, BRep, Unstructured meshes, C++, Open-source

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1. Introduction

Subsurface reservoirs often have a complex spatial organization resulting of sedimentary, diagenetic, magmatic, hydrothermal, and tectonic processes. This motivates the development of flexible geomodeling workflows combining various software and using unstructured grids to compute 3D model queries (e.g. Apel, 2006; Pouliot et al., 2008), simulate contaminant transport (e.g. Blessent et al., 2009), flow in abandoned mines (e.g. Collon et al., 2015), flow in fractured rocks (e.g. Paluszny et al., 2007), seismic waves (e.g. Casarotti et al., 2007), joint gravity and seismic inversion (e.g. Lelievre et al., 2012), transient electromagnetism (e.g. Zehner et al., 2015), model CO_2 storage (e.g. Park et al., 2014), or magmatic intrusion thermal behavior (e.g. Liu et al., 2012). Four main types of software may be distinguished:

- Geomodelers create 3D subsurface models from the available observations, generally by building surfaces bounding geological objects (see Caumon et al. (2009)).
- Meshing software create a spatial discretization of modeled objects. They are generally developed for CAD models without considering geological specificities.
- Numerical solvers solve the partial differential equations governing the subsurface physical processes.
- Scientific visualization software focus on performance, usability, and perception. They help geoscientists to interpret and communicate their results.

Whether software choices be motivated by scientific and technological reasons or by more pragmatic reasons (user proficiency, code availability, time, or budget), geoscientists need to adapt to each software specific constraints and vocabulary. This is exemplified by the recurrent development of file conversion tools, a challenge encountered in all the above cited studies. Beyond this technical challenges of file conversion, communication between software functionalities should also be improved to support new scientific and methodological advances such as a better integration of meshing modules and computational codes (Jackson et al., 2015).

We introduce RINGMesh, an open-source programming library for manipulating discretized geological models, to help the community address these challenges. RINGMesh is neither a geomodeler, nor a meshing software, nor a solver, nor an extensive visualization software. It is designed (i) to ease the integration of these software in flexible geomodeling workflows and (ii) to be a base for the development of new geomodeling, meshing, solver, and visualization software. From this point of view it is similar to the programming library MLSTK (Garimella, 2004). RINGMesh provides a data structure for discretized 3D structural models and implementations of functionalities to import, check the validity, make topological and geometrical requests, store attributes on vertices, edges, facets, and cells of the discretization, visualize a model, export the model to solvers (Fig. 1). Our objective is to share code which we believe will be useful for researchers working with discretized geological models, preventing the re-implementation of similar codes and gaining time to work on real research goals.

After detailing RINGMesh specifications (Sec. 2), we provide a description of the geological model representation used in RINGMesh in Sec. 3. In Section 4, we highlight important features of the current implementation (version 3.0). Finally, we show how RINGMesh can be used to import a discretized structural model, check its validity, generate a tetrahedral mesh using Tetgen (Si, 2015), and visualize the resulting mesh (Sec. 5).



Figure 1: RINGMesh 3.0 main features. Supported file formats are listed in Table 1.

2. Specifications

RINGMesh is a C++ open-source programming library that implements classes to manipulate 3D geological models.

Inputs. The inputs of RINGMesh are discretized 3D geological models. The models can either be defined by their boundary surfaces (polygonal meshes) or be volumetrically meshed (tetrahedra, hexahedra, prisms, and pyramids cells). They can be complete structural models built in a geological modeling software to which topological and geological information is attached, or raw discretizations (e.g. *.stl*). In that case, topological information is recovered by RINGMesh. The formats supported by RINGMesh 3.0 are given Table 1.

Outputs. RINGMesh 3.0 implements functionalities to check the validity of discretized 3D models, visualize the models, and export them in various file formats. RINGMesh implements a file format converter (see Table 1). For example outputs of Skua-Gocad (Paradigm, 2016) can be converted to Code Aster (EDF, 2016) input file format.

Programming Interface. RINGMesh API is designed to be easy to use with well-documented classes and functions, easy to integrate in another software, lightweight and efficient. The most part of the C++ classes, functions, and parameters are documented following the Doxygen standard (Van Heesch, 2016).

License and code distribution. The documented code is distributed under the modified BSD license¹ and is freely available through the web-based service Bitbucket at https://bitbucket.org/ring_team/ringmesh.

¹https://en.wikipedia.org/wiki/University_of_Illinois/NCSA_Open_Source_License

Extension	Software	Surface	Volume	Input	Output	Reference	
gm	RINGMesh	×	×	×	×		
mesh/meshb	LM6	Х	Х	Х	х	(Marechal Loic, 2016)	
ts	Skua-Gocad	×		×	×	(Paradigm, 2016)	
ml	Skua-Gocad	×		×	×	(Paradigm, 2016)	
<i>so</i>	Skua-Gocad	×	×	×	×	(Paradigm, 2016)	
fac	CUBIT	×			×	(Casarotti et al., 2007)	
vtk	VTK	×	×		×	(Kitware, 2016)	
pvd, vtp	Paraview	×			×	(Henderson, 2004)	
mail	Aster	×	×		×	(EDF, 2016)	
inp	Abaqus	×	×		×	(Dassault Systemes, 2016)	
asc/dat	CSMP++	×	×		×	(Paluszny et al., 2007)	
gprs	GPRS		×		×	(Cao, 2002)	
smesh	Tetgen	×			×	(Si, 2015)	
node/ele/neigh	Tetgen		×		×	(Si, 2015)	
msh	Gmsh	×	×		×	(Geuzaine and Remacle, 2009)	
html		×			×	`	
obj		×		×	×		
ply		×		×	×		
off		×		×	×		
stl		×		×	×		

Table 1: Supported file formats for geological models in RINGMesh (version 3.0). All inputs and outputs are discretized models.

Platforms. RINGMesh has been compiled on Linux (GCC 4.4 to 4.8) and Windows (Visual Studio 2010 to 2015), for 64 bits platforms only. We provide configuration files using the cross platform configuration tool CMake (CMake, 2016).

Dependencies. All dependencies are shipped with RINGMesh. The most important one is the geometric algorithm library Geogram (Levy, 2016) (see also Sec. 4.1). It provides the mesh implementation used in RINGMesh, mesh repair functions, search structures, support for various surface and volumetric mesh file formats. We also use zlib (Gailly and Adler, 2016) for in-memory compression and decompression of the input and output files.

3. Geological models in RINGMesh

In geomodeling and in computer aided design (CAD), 3D models can be defined using a Boundary Representation (BRep): each volume (or region) is bounded by a set of surfaces, each surface is bounded by a set of lines, and each line is bounded by two end points. In RINGMesh, we adopted a simple representation similar to the one used in Gmsh (Geuzaine and Remacle, 2009). A geological model is built as sets of entities. The base entities define completely the topology and geometry of the model, while the geological entities define its geological features (Fig. 2). Several alternative computer representations for such models have been proposed in the literature, see for instance Caumon et al. (2004) and the references therein.

3.1. Topological entities

Base entities. Four base entities constitute the BRep model: Corner (dimension 0), Line (dimension 1), Surface (dimension 2), and Region (dimension 3). Each base topological entity is restricted to be a simply connected manifold of arbitrary genus. Simply connected means that the entity has a



Figure 2: Representation of geological models in RINGMesh: base entities and geological entities.

unique connected component (any two points of the entity can be connected by a path contained in the entity), manifold means that the entity does not contain non-manifold point (for example points at a T intersection). Arbitrary genus means that an entity may have holes and internal boundaries.

Adjacencies in the model are represented with a bi-directional data structure: each entity stores a list of upward adjacencies and a list of downward adjacencies. A specific object, the Universe, stores the extension of the model.

- A Region is bounded by a set of oriented Surfaces.
- A Surface is either closed (no boundary) or bounded by a set of Lines and is incident to one or two Regions.
- A Line is either closed or bounded by one or two Corners (closed Lines are cut at one of their vertices), and is incident to at least one Surface.
- A Corner is incident to at least one Line.

The corresponding data model can be represented graphically by:

$$Corner \xleftarrow{1..n}_{1 \text{ or } 2} Line \xleftarrow{1..n}_{0..n} Surface \xleftarrow{1 \text{ or } 2}_{1..n} Region$$

Geological entities. Geological features (faults, horizons, fault-horizon contact, stratigraphic layers, etc.) are represented by geological entities. Each geological entity is a group of base entities to which are associated a name and a geological feature recording its role in the model (normal fault, reverse fault, horizon, unconformity, boundary of the model). In the current implementation of RINGMesh (version 3.0), three geological entities are represented: Contact, Interface, and Layer. Each Contact corresponds to a group of Lines, each Interface to a group of Surfaces, and each Layer to a group of Regions:

$$Line \xleftarrow{0 \text{ or } 1}{1 \dots n} Contact$$

$$Surface \xleftarrow{0 \text{ or } 1}{1 \dots n} Interface$$

$$Region \xleftarrow{0 \text{ or } 1}{1 \dots n} Layer$$

Adjacency relationships between geological entities are not stored. Contrary to the list of base entities, the number of types of geological entities is not fixed, and new geological entities can be implemented and added to the model. Note that geological entities are not mandatory to define a 3D model in RINGMesh and that non geological-models, or geological models for which geological features are not available, can also be manipulated.

3.2. Geometrical representation

In RINGMesh, the geometry of all base entities is represented by a mesh of the same dimension as the entity. Each Corner corresponds to a 3D position. Each Line is represented by a set of adjacent segments, and each Surface by a polygonal surface mesh. Regions can either be defined by their oriented boundary Surfaces, or by a volumetric mesh. To ensure a correct definition of the model, the geometry of the entities should enforce two conditions: (i) the boundary of each entity is a union of entities of lower dimension and (ii) the intersection of two entities is a union of entities of equal or lower dimension. These conditions are the same than those required to have a Piecewise Linear Complex (PLC), the BRep representation used in Tetgen (Si, 2015).

3.3. Validity

Before any manipulation or processing of a discretized geological model, one must be sure that this model is internally consistent. Without this verification, problem identification and debugging of dependent applications is very difficult and cumbersome. Indeed the visual inspection of a 3D model is generally not sufficient to check its validity. The validity of a model is tightly linked to the chosen representation, so validity criteria in RINGMesh are close but not identical to other ones, e.g. Sakkalis et al. (2000).

Base entity validity. Before all, a valid model should be constituted of valid individual entities. First, we check that all model entity discretizations are valid and conformal meshes, i.e. they are defined by a set of elements (vertices, edges, facets, and cells) such that (i) the interior of each element is not empty, and (ii) the intersection of two elements is either empty or is an entity common to their boundaries (Fig. 3c.&d.) (the reader is referred to Frey and George (2000) for complete definitions). Empty elements are typically edges, facets, or cells incident twice to the same



point (Fig. 3b.). Second, a base entity should not contain any non-manifold point (Fig. 3e.), and should have a unique connected component. Finally, Regions defined by their boundary surfaces are to be tight closed volumes.

Model validity. First, a geological model must have a finite extension, i.e. the region defining the exterior of the model must be tight and closed. Second, the boundary of a model entity can only be a set of entities of the model. All the vertices, edges, or facets on the boundary of a Line, Surface, or Region have to be part of a Corner, Line, or Surface. The third validity condition ensures the consistency of the stored entity adjacencies with the geometrical representation: two distinct entities should intersect exclusively along entities of their common boundary. This implies that there is no intersection between two entities except at points that are on their (geometric) boundaries and that are part of a (topological) entity in their boundary.

Geological validity. To have a valid geological model (or Sealed Geological Model), Caumon et al. (2004) propose two additional conditions. The first states that only fault or fracture surfaces might end in a volumetric region and not on another surface of the model. The second condition states that two distinct stratigraphic interfaces cannot cross one another.

The above validity checks are implemented in RINGMesh and permit to ensure that a geological model representation verifies expected properties (see file geo_model_validity.h).

Mesh corrections. Corrective functions are implemented to fix small defects of the mesh and remove: duplicated vertices/edges/facets, isolated vertices, degenerate edges/facets. These functions are adapted and modified from Geogram (Levy, 2016) to allow the duplication of nodes, edges and faces on either sides of geological discontinuities such as fractures and faults (see file geo_model_repair.h). The identification of colocated points involves an epsilon tolerance, while the removal of topological entities is purely combinatorial. Note that in RINGMesh 3.0, there is no complete correction of the BREP representation. The implemented corrections are a subset of those proposed by Alleaume (2009) for CAD models.



Figure 4: 2D example of storage of an unstructured polygonal mesh in 3 arrays.

4. Current implementation highlights

In this section, we shortly describe the core C++ classes of RINGMesh, version 3.0. The code documentation² provides additional details on all algorithms and classes to the interested developers.

4.1. Geogram

To minimize maintenance and capitalize on existing advanced capabilities, RINGMesh uses the mesh data structure implemented in the programming library Geogram (Levy, 2016), distributed under the modified BSD license³.

Geogram, and therefore RINGMesh, supports polygonal surface meshes and mixed-cell volumetric meshes (tetrahedron, hexahedron, triangular prism, and square pyramid). Meshes are represented with an element-node data structure, which is implemented as sets of arrays contiguous in memory. Array means the C++ STL std::vector<> class. Each Mesh has an array of vertices whose coordinates are stored contiguously in memory as an array of double. Polygonal surface facets are encoded by two arrays of indices. The first stores contiguously the indices of vertices of all facets, the second gives the indices of the first and last vertex of each facet in the first array (Fig. 4). Cell encoding is similar to facet encoding: a first array stores the indices of the vertices of all cells, and a second array stores the indices of the first and last corner of each cell.

Using arrays has clear advantages: the code is easy to understand and to maintain, memory usage is minimal, parallelization is easier, objects can be copied using the low level memory copy function memcpy(), they can be loaded (saved) using fread() (fwrite()), and displayed efficiently with a small number of OpenGL instructions. Finally, attributes on the mesh vertices, edges, facets, or cells are simply additional arrays. However as shown by Garimella (2002), the cost of basic mesh modification operations with such a representation is high. In Geogram, to efficiently modify the mesh, these operations are considered at the mesh level and not at the element level, and are applied to a collection of elements and use in place permutation.

4.2. Geological model implementation

In this section, we briefly introduce the C++ classes implementing the geological model representation in the version 3.0 of RINGMesh (see Sec. 3).

²http://www.ring-team.org/ring_dl/public/software/ringmesh/doc/

³Several libraries bundled in Geogram have more restrictive licenses: http://alice.loria.fr/software/geogram/doc/html/geogram_license.html

To each geological model corresponds an instance of the class GeoModel. A GeoModel stores and manages an array of its constitutive entities. All the entities of the model are instance of the GeoModelEntity class, which store basic identification information and a geological feature. The base entities are implemented as classes (Corners, Lines, Surfaces, Regions) derived from the abstract class GeoModelMeshEntity and store their geometrical (mesh) and topological information (adjacencies and incidences). The abstract base class GeoModelGeologicalEntity is derived to implement the concrete geological entity classes (Contact, Interface, Layer).

Input and outputs are handled by the GeoModelIOHandler. Several classes are implemented to modify and/or create GeoModels: the GeoModelEditor and the GeoModelBuilder, which is derived for the different types of supported inputs. A specific one is dedicated to model repairing, GeoModelRepair.

All base entities (Corner, Line, Surface, Region) of the GeoModel are discretized. Their geometry is defined by an unstructured mesh that is stored as a Mesh object. The Mesh class is a wrapper of the class Mesh of Geogram on which the most part of the Geogram functionalities can be used. We also use a global Mesh instance of the whole model which is shared by all entities. This representation is very useful for validity checks, exports to exotic formats, and the recovery of the topology of a set of disconnected conformal surfaces. These operations depend on a consistent global indexing of colocated vertices, edges, and facets of the model (see the implementation of GeoModelBuilderSurface and of is_geomodel_valid()).

4.3. Indexing of mesh elements

As we have seen in Section 4.1, meshes in RINGMesh are represented using an element based strategy that uses arrays of integers to represent the edges, facets, and cells of a mesh. Consequently, manipulating meshes, importing discretized geological models from files, representing meshed geological models, and exporting them means dealing with a lot of indexes. Indeed, requirements on stored information vary a lot between file formats. For example, to export a model to the solver CSMP++ (Paluszny et al., 2007), a numbering is required for each type of cell (tetrahedron, prisms, hexahedron, etc) and in each region of the model. To handle this requirement, the elements of the global Mesh of the whole model are reordered and permuted in-place. Cells are sorted region by region, and type by type in each region.

5. Using RINGMesh

With RINGMesh 3.0 it is possible for various input file formats (see Table 1) to:

- visualize the model and its discretization (Fig. 5 and 6),
- export the model to another file format (Table 1),
- recover the volumetric regions of a surface model,
- check the validity of a model and repair small discretization defects (Section 5.1),
- call an external software to tetrahedralize the model (Sec. 5.2)

All these operations are performed in a matter of seconds (Table 2).

Table 2: Execution timings in seconds for typical tasks performed by RINGMesh 3.0 on a laptop with a 4,00Go RAM, and an Intel i5-4200U processor (2 cores, 1.60GHz). They depend mainly on the total size of the surface and volumetric meshes. The geological models are part of the RINGMesh test dataset and are freely available.

Action	Dataset	File for In	mats Out	Mesh size # facets/cells	Load (s)	Validity check (s)	Facet Int. check (s)	Action (s)	Save (s)
Repair	annot	.ml	.ml	130,417	1.33	0.41	4.67	0.79	1.83
Tetgen	corbi	.ml	.gm	$277,\!113$	2.36	0.72	4.39	50.42	14.00
Construct	modelA6	.mesh	.gm	55,426	0.42	0.21	1.46	0.15	1.00
Convert	modelA4	.so	.gm	$34,\!540$	1.24	0.29	0.32	0	1.42



Figure 5: Unstructured surface and volumetric meshes of the Corbieres geological model visualized with RINGMesh light viewer. a. Surface model (from Caumon et al. (2009)). b. Tetrahedral mesh generated in RINGMesh using Tetgen (Si, 2015).



Figure 6: Mixed element volumetric mesh in RINGMesh. The mesh was generated in an application developed on top of RINGMesh by Botella et al. (2016). The model is courtesy of Total.

5.1. Model validity checking

For most geological models, checking by hand the validity of the 3D model topological and geometrical entities is impossible. For example, the model of the Annot sandstones built by Salles et al. (2011) in Skua-Gocad (Fig. 7a.) contains 1,261 base entities and 125 geological entities. The model is visually consistent but a few local mesh issues break its validity (in the sense discussed in Section 3.3). Using RINGMesh we detect:

- 5 colocated vertices associated to 1 duplicated facet and 8 degenerate facets on Surface #2, resulting in the invalidity of that surface and of the two adjacent regions.
- 2 degenerate Lines (#346 and #397) containing a unique degenerate edge, (2 pairs of colocated vertices) resulting in the invalidity of 2 Surfaces (#44 and #50) each containing a degenerate facet built on this edge.

These degenerate Lines, colocated vertices, degenerate and duplicated facets (Fig. 7c.) can be automatically removed, resulting in a valid model.

Listing 1: Example of C++ source code to load the Corbieres geological model in RINGMesh, mesh it with TetGen, and export the resulting mesh.

```
#include <ringmesh/geomodel/geo_model.h>
#include <ringmesh/geomodel/geo_model_api.h>
#include <ringmesh/geomodel/geomodel_validity.h>
#include <ringmesh/io/io.h>
int main() {
  using namespace RINGMesh ;
  GeoModel model ;
  geomodel_load( "corbieres.ml", model) ;
  if ( is_geomodel_valid ( model ) ) {
     tetrahedralize( model, "TetGen" ) ;
     geomodel_save( model, "corbieres_tetgen.meshb" ) ;
    else {
    Logger::out("Error") << "The loaded model is invalid";
  }
  return 0;
}
```

5.2. Interface to external meshing software

To ease the generation of unstructured meshes of geological models, RINGMesh interfaces external meshing software such as TetGen (Si, 2015) and MG-Tetra⁴ (George et al., 1991) The meshes are constrained, meaning that the facets of the triangulated surfaces are a subset of the generated tetrahedron facets. When well paths are associated to the structural model, the generated meshes can also be conformal to their edges. The main function running the example of Figure 5 is written in Listing 1. The generated volumetric meshes can be exported to various file formats (Table 1). They can also be visualized in the standalone light-weight viewer that is shipped with RINGMesh. The implementation of the viewer relies on the fast graphics provided by Geogram (Sec. 4.1), as displaying a GeoModel means displaying a set of meshes (Fig. 5).

⁴http://www.meshgems.com/volume-meshing-meshgems-tetra.html



Figure 7: Invalid mesh elements and invalid entities detection on the Annot model. a. The Annot geological model (from Salles et al. (2011)) loaded in RINGMesh. b. Three surfaces of the model are invalid: Surface #2 contains 8 degenerate facets, Surface #44 and #50 contain 1 degenerate facets. c. Surface #2 mesh seems to be correct but contains 8 invisible degenerate facets in this area.

6. Conclusion

RINGMesh is a joint effort to factorize in a common library a simple and efficient data model and to ease the tedious tasks of reading and writing files describing geological models in various formats. Since the very first version that loaded the surface models of Skua-Gocad (Paradigm, 2016), and computed complexity measures (Pellerin et al., 2015), the code has been evolving toward an increasingly flexible library. The current version is designed for researchers who develop new geomodeling methods and implement their own software. It is easy to integrate in another code and provides a set of fundamental operations on discretized geological models.

RINGMesh has been used for the development of meshing methods dedicated to geological models (Pellerin et al., 2014a,b; Botella et al., 2016) and was integrated in several workflows to: find appropriate boundary conditions in 3D geomechanical restoration (Chauvin et al., 2016), to perform homogenization for seismic wave propagation (Cupillard et al., 2015), and to determine far-field stress conditions from several borehole observations (Mazuyer et al., 2016). In these applications, RINGMesh met its initial objectives. Namely, it provided a geological data structure suitable for the development of research codes for tetrahedral and hex-dominant meshing (Fig. 6) and finite element computations. It also served to quickly exchange data between geomodeling software, meshing software, and computational codes.

RINGMesh is still a rather young programming library and its functionalities and data structures are still being improved and extended. The main limitation of the version 3.0 of RINGMesh is that the data structures have not been been designed to support modifications of the geological models. This makes the implementation of model modification functionalities complicated. A second limitation is the early stage of development of some functionalities such as exports of some formats and validity checks. These tools are very useful in their present form but improvements and more thorough tests are necessary. Some basic tests are already performed using the continuous integration platform Jenkins⁵. It is however very challenging to check the validity of all exported files.

There are of course many remaining possibilities to extend and improve RINGMesh in order to increase communication between geomodeling software, meshing software, solvers, and visualization software developed or not for geological application. The main directions for future developments of RINGMesh are:

- to support in input and output all widely used file formats in geological modeling, including the open, non-proprietary data exchange format RESQML (Energistics, 2016),
- to check modes against different sets of validity conditions,
- to support model modifications, both topological (e.g. removal/addition of a layer, a fault) and on the meshes (e.g. remesh locally a region),
- to repair invalid models.

RINGMesh is open-source and all participations to the project are very welcome. New developments (import/export functions, bug fixes) can be submitted and easily integrated through the project Bitbucket public repository⁶.

⁵https://jenkins-ci.org

⁶https://bitbucket.org/ring_team/ringmesh

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